

TRIGONOMETRY- 2

CLASS X (2025-26)

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- 1 If $\sin \theta = \cos \theta$, then the value of θ is _____. ($0^\circ \leq \theta \leq 90^\circ$)
- 2 If $\operatorname{cosec} \theta - \cot \theta = \frac{1}{3}$ the value of $(\operatorname{cosec} \theta + \cot \theta)$ is _____.
A) 1 B) 2 C) 3 D) 0
- 3 If $\tan A = \frac{5}{12}$, find the value of $(\sin A + \cos A) \cdot \sec A$.
(a) $\frac{13}{12}$ (b) $\frac{17}{12}$ (c) $\frac{12}{17}$ (d) $\frac{12}{13}$
- 4 If $\tan(A + B) = \sqrt{3}$ and $\tan(A - B) = \frac{1}{\sqrt{3}}$, $0^\circ < A + B \leq 90^\circ$, $A > B$. A and B are _____ and ____.
- 5 $4\cot^2 45^\circ - \sec^2 60^\circ + \sin^2 60^\circ + \cos^2 90^\circ =$ _____.
- 6 If $\sec^2 \theta (1 + \sin \theta) (1 - \sin \theta) = k$, then find the value of k is _____.
- 7 The value of $\frac{1}{5} \sec^2 A - \frac{1}{5} \tan^2 A =$ _____.
A) 5 B) 9 C) $\frac{1}{5}$ D) 0
- 8 If $5 \tan \theta = 4$, evaluate $\frac{5 \sin \theta - 3 \cos \theta}{5 \sin \theta + 2 \cos \theta}$
- 9 Find the value of x , if $\tan 3x = \sin 45^\circ \cdot \cos 45^\circ + \sin 30^\circ$.
- 10 In ΔABC , right angled at B, $AB = 5$ cm and $\sin C = \frac{1}{2}$. Determine the length of side AC
- 11 If $\sec \theta = \frac{25}{7}$, find the values of $\tan \theta$ and $\operatorname{cosec} \theta$.
- 12 In ΔABC , right angle at B, if $AB = 12$ cm and $BC = 5$ cm, find
(i) $\sin A$ and $\tan A$, (ii) $\sin C$ and $\cot C$.
- 13 Given $A = 30^\circ$, verify $\sin 2A = 2 \sin A \cos A$.
- 14 If $\tan \theta = \frac{1}{\sqrt{3}}$, ($0^\circ \leq \theta \leq 90^\circ$) then evaluate $\frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta}$
- 15 If $\sin(A - B) = \frac{1}{2}$, $\cos(A + B) = \frac{1}{2}$, find A and B.
- 16 Simplified form of $(1 + \tan^2 \theta) (1 - \sin \theta) (1 + \sin \theta)$ is _____.
A) 1 B) $\frac{1}{2}$ C) $\cot^2 \theta$ D) $\tan^2 \theta$
- 17 Find the value of x if $\cos 2x = \sin 60^\circ \cdot \cos 30^\circ - \cos 60^\circ \cdot \sin 30^\circ$.
A) 60° B) 36° C) 27° D) 30°
- 18 The value of $\frac{1 - \sin 60^\circ}{\cos 60^\circ} =$ _____
- 19 If $\sec \theta - \tan \theta = \frac{1}{2}$ the value of $(\sec \theta + \tan \theta)$ is _____.
- 20 If $\tan A = \frac{5}{12}$, find the value of $(\sin A + \cos A) \cdot \sec A$.

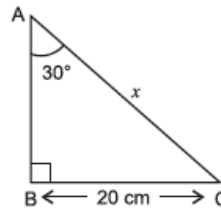
21 If $\cot \theta = \frac{7}{8}$ evaluate $\frac{(1+\sin \theta)(1-\sin \theta)}{(1+\cos \theta)(1-\cos \theta)}$

22 If $\sin \theta = \frac{1}{3}$, then find the value of $(2 \cot^2 \theta + 2)$

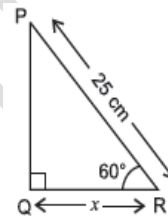
23 If $3x = \operatorname{cosec} \theta$ and $\frac{3}{x} = \cot \theta$, find the value of $3\left(x^2 - \frac{1}{x^2}\right)$

24 If $\sin \theta = x$ and $\sec \theta = y$, then find the value of $\cot \theta$.

25 Find the value of x from the figure.



26 Find the value of x from the figure.



27 Evaluate: $3 \cot^2 60^\circ + \sec^2 45^\circ$

28 If $\sin A = \frac{\sqrt{3}}{2}$ find the value of $2 \cot^2 A - 1$.

29 If $\cos(40^\circ + x) = \sin 30^\circ$, find the value of x .

30 By taking $A = 30^\circ$, evaluate $4\cos^3 A - 3\cos A$

31 If $\tan x = \sin 45^\circ \cos 45^\circ + \sin 30^\circ$ then $x = \underline{\hspace{2cm}}$.

32 If $A = 60^\circ$ and $B = 30^\circ$, verify that $\sin(A + B) = \sin A \cos B + \cos A \sin B$

33 If $a \cos \theta - b \sin \theta = x$ and $a \sin \theta + b \cos \theta = y$. Prove that $a^2 + b^2 = x^2 + y^2$.

34 Prove that : $\frac{\sin \theta + \cos \theta}{\sin \theta - \cos \theta} + \frac{\sin \theta - \cos \theta}{\sin \theta + \cos \theta} = \frac{2 \sec^2 \theta}{\tan^2 \theta - 1}$

35 Prove that : $\frac{\cos A}{1 + \sin A} + \frac{1 + \sin A}{\cos A} = 2 \sec A$

36 The value of $\frac{1}{2} \sin^2 A + \frac{1}{2} \cos^2 A = \underline{\hspace{2cm}}$.

37 If $\tan(A + B) = \sqrt{3}$, $\tan(A - B) = \frac{1}{\sqrt{3}}$, $0 < A + B < 90$, $A > B$, find A and B .

38 If $\sec^2 \theta (1 + \sin \theta)(1 - \sin \theta) = k$, then find the value of k .

39 If $6x = \sec \theta$ and $\frac{6}{x} = \tan \theta$, find the value of $9\left(x^2 - \frac{1}{x^2}\right)$

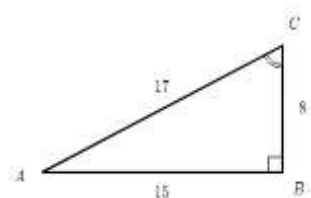
40 If $3 \tan \theta = 4$, evaluate $\frac{5 \sin \theta - 3 \cos \theta}{5 \sin \theta + 2 \cos \theta}$

41 In a triangle ABC, right angled at B, the ratio of AB to AC is $1 : \sqrt{2}$. Find the value of $\frac{2 \tan A}{1 + \tan^2 A}$

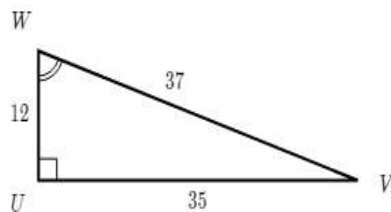
42 If $A = 60^\circ$ and $B = 30^\circ$, verify that: $\sin(A - B) = \sin A \cos B - \cos A \sin B$.

- 43 If $7\sin^2\theta + 3\cos^2\theta = 4$, then show that $\tan\theta = \frac{1}{\sqrt{3}}$
- 44 If $\sin\theta = \frac{m}{n}$, find the value of $\frac{\tan\theta+4}{4\cot\theta+1}$
- 45 Prove that : $(1 + \cot\theta - \operatorname{cosec}\theta)(1 + \tan\theta + \sec\theta) = 2$
- 46 Prove that: $\frac{\tan\theta+\sec\theta-1}{\tan\theta-\sec\theta+1} = \frac{1+\sin\theta}{\cos\theta}$
- 47 Prove that: $\frac{1}{(\sec x - \tan x)} - \frac{1}{\cos x} = \frac{1}{\cos x} - \frac{1}{(\sec x + \tan x)}$
- 48 Evaluate : $4 \cot^2 45^\circ - \sec^2 60^\circ + \sin^2 60^\circ + \cos^2 90^\circ$.
- 49 Find the value of x if $\tan 3x = \sin 45^\circ \cdot \cos 45^\circ + \sin 30^\circ$.
- 50 Taking $A = 30^\circ$, verify that $\cos 3A = 4\cos^3 A - 3\cos A$
- 51 Prove that: $\frac{\cot\theta+\operatorname{cosec}\theta-1}{\cot\theta-\operatorname{cosec}\theta+1} = \frac{1+\cos\theta}{\sin\theta}$
- 52 Prove that: $\frac{\sin\theta+\cos\theta}{\sin\theta-\cos\theta} + \frac{\sin\theta-\cos\theta}{\sin\theta+\cos\theta} = \frac{2}{\sin^2\theta - \cos^2\theta}$
- 53 Prove that: $\sin^4\theta + \cos^4\theta = 1 - 2\sin^2\theta \cos^2\theta$.
- 54 Simplify: $(1 + \tan^2\theta)(1 - \sin\theta)(1 + \sin\theta)$.
- 55 If $\sec\theta + \tan\theta = m$ and $\sec\theta - \tan\theta = n$, find the value of $\sqrt{mn}$.
- 56 If $\sin\theta + \cos\theta = p$ and $\sec\theta + \operatorname{cosec}\theta = q$, show that $q(p^2 - 1) = 2p$.
- 57 Prove the following identity: $\frac{\sin\theta}{1-\cos\theta} + \frac{\tan\theta}{1+\cos\theta} = \sec\theta \cdot \operatorname{cosec}\theta + \cot\theta$
- 58 Prove the following identity : $\cos^4 A - \cos^2 A = \sin^4 A - \sin^2 A$
- 59 Prove the following identity : $\sin^4 A + \cos^4 A = 1 - 2\sin^2 A \cos^2 A$
- 60 Prove that: $\frac{\cos\theta}{1-\sin\theta} = \frac{1+\sin\theta}{\cos\theta}$
- 61 Prove the following identity: If $\cos\theta - \sin\theta = 1$, show that $\cos\theta + \sin\theta = 1$ or -1 .
- 62 If $a \cos\theta - b \sin\theta = x$ and $a \sin\theta + b \cos\theta = y$. Prove that $a^2 + b^2 = x^2 + y^2$.
- 63 If $A = 60^\circ$ and $B = 30^\circ$, verify that $\cos(A - B) = \cos A \cos B + \sin A \sin B$.
- 64 Determine the value of x such that $2 \operatorname{cosec}^2 30^\circ + x \sin^2 60^\circ - \frac{3}{4} \tan^2 30^\circ = 10$
- 65 If $6x = \sec\theta$ and $\frac{6}{x} = \tan\theta$, find the value of $9\left(x^2 - \frac{1}{x^2}\right)$
- 66 Prove that $(\operatorname{cosec}\theta - \cot\theta)^2 = \frac{1-\cos\theta}{1+\cos\theta}$
- 67 If $x = a \cos\theta + b \sin\theta$, $y = a \sin\theta - b \cos\theta$, prove that $x^2 + y^2 = a^2 + b^2$
- 68 Prove that: $\frac{\tan A}{\sec A - 1} + \frac{\tan A}{\sec A + 1} = 2 \operatorname{cosec} A$.
- 69 If $2 \cos\theta - \sin\theta = x$ and $\cos\theta - 3 \sin\theta = y$, prove that $2x^2 + y^2 - 2xy = 5$.
- 70 If $\cos\theta - \sin\theta = \sqrt{2} \sin\theta$, prove that $\theta + \sin\theta = \sqrt{2} \cos\theta$

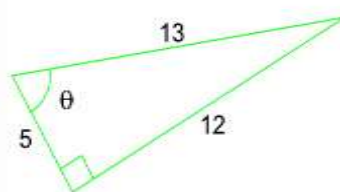
71 Find $\sin C$, $\cos C$



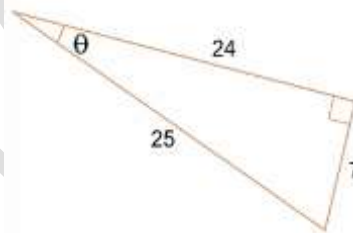
72 Find $\sin W$, $\tan W$



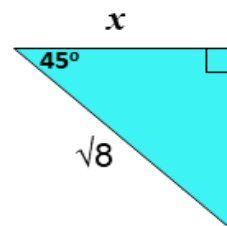
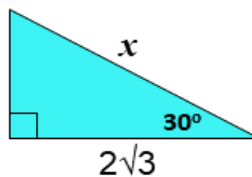
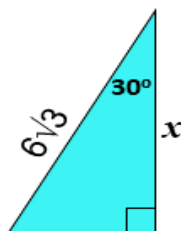
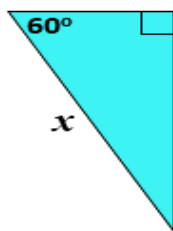
73 Find $\tan \theta$, $\cos \theta$



74 Find $\sec \theta$, $\operatorname{cosec} \theta$



75 Find x



76 Taking $A = 30^\circ$, verify that i) $\sin 2A = 2\sin A \cos A$ ii) $\cos 2A = 2\cos^2 A - 1$

iii) $\sin 3A = 3\sin A - 4\sin^3 A$ iv) $\tan 2A = \frac{2\tan A}{1-\tan^2 A}$ v) $\cos 3A = 4\cos^3 A - 3\cos A$

77 1. If $A = 60^\circ$ and $B = 30^\circ$, verify that

i) $\sin(A + B) = \sin A \cos B + \cos A \sin B$ (Ans: 1)

ii) $\cos(A + B) = \cos A \cos B - \sin A \sin B$ (Ans: 0)

iii) $\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$ (Ans: $\frac{1}{\sqrt{3}}$)