SUJITHKUMAR KP

SAMPLE PAPER
PERIODIC TEST – 2
Class: X

Subject: Mathematics (041) M.M : 80
Date : 01- 09 - 2025 Time : 3 Hours

General Instructions:
1. This Question paper contains - five sections A, B, C, D and E. Each section is compulsory.
2. Section A has 18 MCQ's and 02 Assertion – Reason based questions of 1 mark each.
3. Section B has 5 Very Short Answer (VSA) – type questions of 2 marks each.
4. Section C has 6 Short Answer (SA) – type questions of 3 marks each.
5. Section D has 4 Long Answer (LA) – type questions of 5 marks each.
6. Section E has 3 source based/case based/passage based/integrated units of assessment of 4 marks each with sub-parts.
7. All Questions are compulsory. However, an internal choice in 2 questions of 5 marks, 2 questions of 3 marks and 2 Questions of 2 marks has been provided. An internal choice has been provided in the 2 marks questions of Section E.
8. Draw neat figures wherever required. Take $\pi = \frac{22}{7}$ wherever required if not stated.

SECTION - A

1. The next term of the AP $\sqrt{18}, \sqrt{50}, \sqrt{98}, \ldots\ldots\ldots$ (1)
(A) $\sqrt{152}$ (B) $\sqrt{160}$ (C) $\sqrt{121}$ (D) $\sqrt{162}$

2. If $tan\theta = 1$ and $sin\alpha = \frac{1}{\sqrt{2}}$, find the value of $\cos(\theta + \alpha)$, θ and α are both acute angles. (1)
(A) 0 (B) 1 (C) $\frac{1}{2}$ (D) $-\frac{1}{2}$

3. The sum of exponents of prime factors in the prime factorisation of 250 is _____ (1)
(A) 3 (B) 4 (C) 5 (D) 6

4. If $tan\left(\frac{5\theta}{2}\right) = \sqrt{3}$ and θ is acute, then find the value of 2θ. (1)
(A) 40° (B) 24° (C) 48° (D) 120°

5. In triangles ABC and DEF, $\frac{AB}{DE} = \frac{BC}{FD}$, then they will be similar, when___ (1)
(A) $\angle B = \angle E$ (B) $\angle A = \angle D$ (C) $\angle B = \angle D$ (D) $\angle A = \angle F$

6. If the roots of quadratic equation $ax^2 + bx + c = 0$ are equal in magnitude but opposite in sign then find the value of b. (1)
(A) -2 (B) 2 (C) 0 (D) -1

7. The perimeters of two similar triangles are 25 cm and 15 cm respectively. If one side of first triangle is 9 cm., what is the corresponding side of the other triangle ? (1)
(A) 5.4cm (B) 4 cm (C) $\frac{5}{3}$ cm D) 3cm

8. If $tan\theta = \frac{a}{b}$, then find the value of $\frac{a\sin\theta + b\cos\theta}{a\sin\theta - b\cos\theta}$ is _____ (1)
(A) $\frac{a^2-b^2}{a^2+b^2}$ (B) $\frac{a^2+b^2}{a^2-b^2}$ (C) $\frac{a}{a^2+b^2}$ (D) $\frac{b^2}{a^2+b^2}$

9. Quadratic polynomial whose zeros are $3 - 2\sqrt{3}$ and $3 + 2\sqrt{3}$ is _____ (1)
(A) $x^2 - 6x - 3$ (B) $x^2 - 6x + 3$
(C) $x^2 + 6x - 3$ (D) $x^2 + 3x - 6$

10. Line joining $(-1, 1)$ and $(5, 7)$ is divided by a line $x + y = 4$ in the ratio of _____ (1)
(A) 1:2 (B) 1:3 (C) 3:4 (D) 1:4

11. Half the perimeter of a rectangular garden, whose length is 12 m more than its width is 60 m. Find the length of the garden. (1)
(A) 36 (B) 20 (C) 18 (D) 72

12. If the opposite angular points of a square are $(4, 3)$ and $(2, -3)$ then the side of the square is___ (1)
(A) 40 (B) 20 (C) $\sqrt{20}$ (D) $\sqrt{40}$

13. Determine k for which the system of equations has infinite solutions: $4x + y = 3$ and $8x + 2y = 5k$. (1)
(A) $\frac{5}{6}$ (B) 1 (C) $\frac{6}{5}$ (D) $\frac{3}{5}$

14. There are 576 boys and 448 girls in a school that are to be divided into equal sections of either boys or girls alone. The total number of sections thus formed are: (1)
(A) 15 (B) 16 (C) 17 (D) 20

15. If the prime factorisation of a natural number N is $2^4 \times 3^4 \times 5^3 \times 7$ find the number of zeros in N is ____. (1)
(A) 1 (B) 2 (C) 3 (D) 4

16. If $px^2 + 3x + q = 0$ has two roots $x = -1$ and $x = -2$, then $q - p =$ ___ (1)
(A) 1 (B) -1 (C) 3 (D) 2

17. If the distance between the points $(4, p)$ and $(1, 0)$ is 5 units, then the value of p is _____. (1)
(A) 4 only (B) ± 4 (C) -4 only (D) 0

18. The quadratic equation $4x^2 + 6x + 3 = 0$ has _____ (1)
(A) two distinct real roots (B) two equal real roots
(C) no real roots (D) more than 2 real roots

In the following questions 19 and 20, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices.
(A) Both A and R are true and R is the correct explanation of A.
(B) Both A and R are true but R is not the correct explanation of A.
(C) A is true but R is false.
(D) A is false but R is true.

19. **Assertion (A):** The coordinates of a point P which divides the line segment joining the points A(– 2, 3) and B(4, 7) internally in the ratio $\frac{4}{7}$ is $\left(\frac{49}{11}, \frac{2}{11}\right)$. (1)
Reason (R): The coordinates of the point $P(x, y)$ which divides the line segment joining the points $A(x_1, y_1)$ and $B(x_2, y_2)$ in the ratio $m:n$ is $x = \frac{mx_2 + nx_1}{m+n}$, $y = \frac{my_2 + ny_1}{m+n}$.

20. **Assertion (A):** The graph of the linear equations $x + 3y = 6$, $2x - 3y = 12$ gives a pair of intersecting lines. (1)
Reason (R): A pair of linear equations in two variables in x and y, $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$ has a unique solution if $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ gives a pair of intersecting lines.

SECTION - B

21. If $sec\,\theta - tan\,\theta = \frac{1}{2}$, find the value of $(sec\,\theta + tan\,\theta)$. (2)

OR

Prove that: $\frac{sinA - sinB}{cosA + cosB} + \frac{cosA - cosB}{sinA + sinB} = 0$

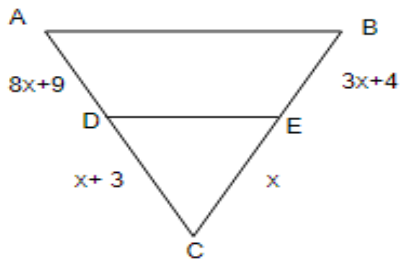
22. Determine the set of values of k for which the given quadratic equation has real roots: (2)
$2x^2 + 3x + k = 0$.

OR

Had Ajita scored 10 more marks in her mathematics test out of 30 marks, 9 times these marks would have been the square of her actual marks. How many marks did she get in the test?

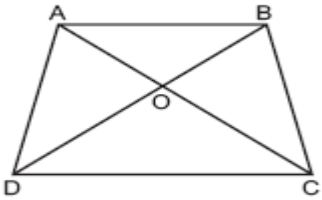
23. Find the 12^{th} term from the end of the following arithmetic progression: 3, 5, 7, 9, …. 201 (2)

24. What value(s) of x will make $DE \parallel AB$ in the given figure? (2)



OR

In the given figure , $\frac{AO}{OC} = \frac{BO}{OD} = \frac{1}{2}$ and AB = 4 cm. Find the value of DC..



25. Find the ratio in which the point $(2,\ y)$ divides the line segment joining the point $A\ (-2, 2)\ and\ B(3, 7)$. Also find the value of y. (2)

SECTION -C

26. Find the values of $\alpha\ and\ \beta$ for which the following system of linear equations has infinite solutions (3)
$2x + 3y = 7\ ,\quad 2\alpha x + (\alpha + \beta)y = 28.$

27. If a and b are roots of the equation $2x^2 + 7x + 5 = 0$ then write a quadratic equation whose roots are $2a + 3\ and\ 2b + 3$. (3)

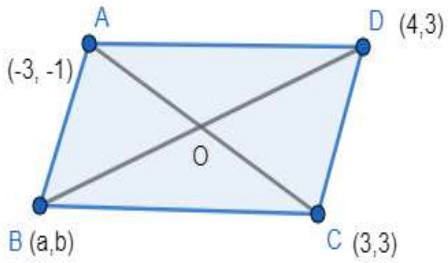
OR

In a flight of 2800 km, an aircraft was slowed down due to bad weather. Its average speed is reduced by 100 km/h and time increased by 30 minutes. Find the original duration of the flight.

28. The sum of three numbers of an AP is 27 and their product is 405. Find the numbers. (3)

29. Show that 21^n cannot end with the digits 0, 2, 4, 6 and 8 for any natural number n. (3)

30. If four vertices of a parallelogram taken in order are $(-3, -1), (a, b), (3, 3)\ and\ (4, 3)$, then find the ratio $a : b$ (3)



OR

Find the point on y-axis which is equidistant from the points (5, – 2) and (–3, 2).

31. If the roots of the equation $12x^2 + mx + 5 = 0$ are in the ratio 3 : 2, then m (3)

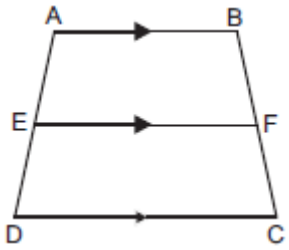
SECTION –D

32. If α and β are zeroes of $3x^2 - 6x + 4$, then find the value of : $\left(\frac{\alpha}{\beta} + \frac{\beta}{\alpha}\right) + 2\left(\frac{1}{\alpha} + \frac{1}{\beta}\right) + 3\ \alpha\ \beta$ (5)

OR

If α and β are roots of $ax^2 + bx + b = 0$, then find the value of $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} + \sqrt{\frac{b}{a}}$.

33. If a line is drawn parallel to one side of a triangle, the other two sides are divided in the same ratio, prove it. Use this result to prove the following : (5)
In the given figure, if ABCD is a trapezium in which $AB \parallel DC \parallel EF$, then $\frac{AE}{ED} = \frac{BF}{FC}$



34. Solve for x *and* y, $\quad \sqrt{2}x + \sqrt{3}y = 5 \quad , \quad \sqrt{3}x - \sqrt{8}y = -\sqrt{6}.$ (5)

35. Prove that: $\frac{tan\theta + sec\theta - 1}{tan\theta - sec\theta + 1} = \frac{1+sin\theta}{cos\theta}$ (5)

OR

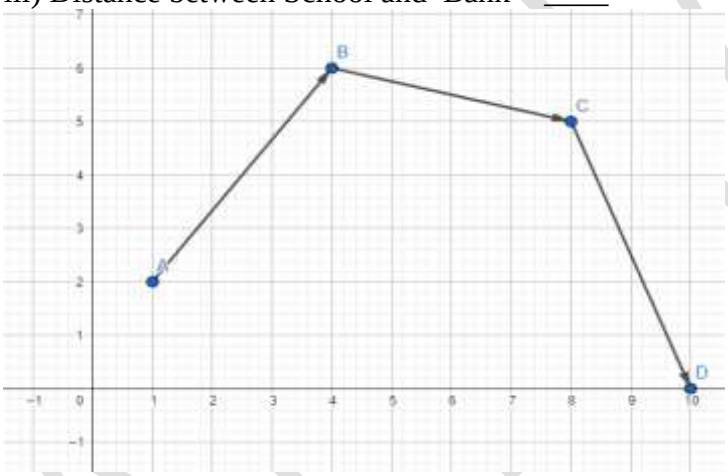
If $sin\,\theta + cos\,\theta = p$ and $sec\,\theta + cosec\,\theta = q$, show that $q(p^2 - 1) = 2p$.

SECTION – E

36. Aditya starts walking from his house to office. Instead of going to the office directly, he goes to the school drop his daughter first and there to a bank and reaches the office. Assume that all distances covered are in straight line. If the house is situated at A (1, 2) . School at B (4, 6), The bank at C(8,5) and the office at D (0,10). Distances are in km.
i) Distance between House and School = _____ (1)
ii) Actual distance between House and office = _____ (1)
iii) The mid point of AC =_____ (2)

OR

iii) Distance between School and Bank = ____

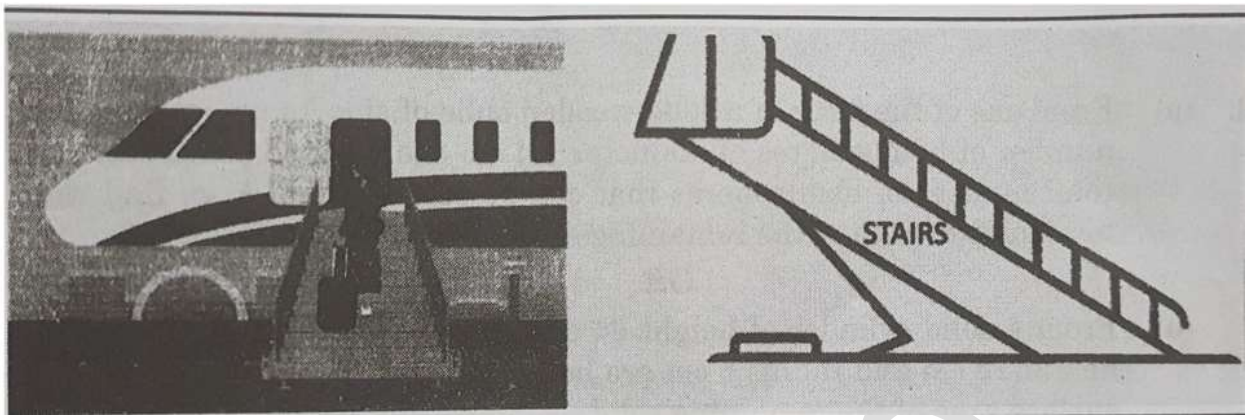


37. Raj and Ajay are very close friends. Both the families decide to go to Rann of Kutch by their own cars. Raj's car travels at a speed of x km/h while Ajay's car travels 5 km/h faster than Raj's car. Raj took 4 hours more than Ajay to complete his journey of 400 km.
i) What will be the distance covered by Ajay's car in two hours? (1)
ii) Which of the following quadratic equation describe the speed of Raj's car? (1)
iii) How much time took Ajay to travel 400 km?.

OR (2)

iii) What is the speed of Raj's car?

38. Passengers boarding stairs, sometimes referred to as boarding ramps, stair cars or air craft steps, provide a mobile means to travel between the air craft doors and the ground. Larger air craft have door sills 5 to 20 feet (1 foot = 30 cm) high. Stairs facilitate safe boarding and de- boarding.



An air craft has a door sill at a height of 15 feet above the ground. A stair car is placed at a horizontal distance of 15 feet from the plane.

Based on the given information, answer the following questions given in part (i) and (ii).

(i) Find the angle at which the stairs are inclined to reach the door sill 15 feet high above the ground. (1)

(ii) Find the length of the stairs used to reach the door sill. (1)

Further, answer any **one** of the following questions

(iii) (a) If the 20 feet long stairs is inclined at an angle of $60°$ to reach the door sill, then find the height of the door sill above the ground ($\sqrt{3} = 1.732$) (2)

OR

(b) What should be the shortest possible length of the stairs to reach the door sill of the plane 20 feet above the ground , if the angle of elevation cannot exceed $30°$? Also find the horizontal distance of base of the stair car from the plane.

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